Reg. No. :

Fifth Semester B.Sc. Degree Examination, December 2022

First Degree Programme Under CBCSS

Statistics

Open Course

ST 1551.4 : OFFICIAL STATISTICS

(2018 Admission Onwards)

Time : 3 Hours

Max. Marks: 80

P - 2603

SECTION - A

Answer all questions. Each question carries 1 mark.

1. What is the full form of MOSPI?

2. Define vital statistics.

3. Define stable population.

4. Define index numbers.

5. What is price relative?

6. Define time series.

7. The geometric mean of Laspeyre's and Paasche's price indices is also known as

8. If I_x is the number of persons living at the age x and L_x the number of persons living in the mid of x and (x+1) years, then the relation between I_x and L_x is

P.T.O.

Periodic changes in a business time series are called ______.

10. Quarterly fluctuations observed in time series ______ represent variation.

 $(10 \times 1 = 10 \text{ Marks})$

SECTION - B

Answer any eight questions. Each question carries 2 marks.

11 Explain semi-average method in time series.

12 What are the components of time series?

- 13. What are the normal equations to fit a straight line y = a + bx?
- 14. Define moving average.
- 15. What is mean by cyclic variations in time series analysis?
- 16. Define secular trend of a time series.
- 17. What are the measures of mortality to express death rates?
- 18. Define infant mortality rate.
- 19. List important statistical organizations in India.
- 20. Distinguish between primary and secondary data.
- 21. What are the different types of fertility rates?
- 22. Give any two limitations of index numbers.
- 23. Explain briefly the concept of cost of living index number.
- 24. What is time reversal test?
- 25. Give the formula for Laspeyre's and Paasche's index.

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26. What is quantity relative?

(8 × 2 = 16 Marks)

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SECTION - C

Answer any six questions. Each question carries 4 marks.

- 27. Distinguish between additive and multiplicative models of time series.
- 28. Elucidate the uses and limitations of time series analysis
- 29. What are the different methods to identify trend in time series?
- 30. What are the methods mainly used to determine seasonal variations?
- 31. Give two examples each to (a). Seasonal variation (b). Irregular variation.
- 32. Why index numbers are called economic barometers? Explain.
- 33. Distinguish between simple index number and weighted index number. Mention any two applications of weighted index number.
- 34. What are the main steps in construction of cost of living index numbers?
- 35. Distinguish between Weighted aggregative index and Weighted average of relatives.
- 36. Describe various components of a life table. How is the expectation of life at birth determined from a life table?
- 37. What are the main functions of NSSO?
- 38. Define and compare various measures of fertility.

 $(6 \times 4 = 24 \text{ Marks})$

SECTION - D

Answer any two questions. Each question carries 15 marks.

- 39. Why Fisher's index number known as ideal Index Number?
- 40. Describe the steps involved in Ratio to moving average method and link relative method of measuring seasonal indices.
- 41. Describe main features of the statistical system in India.

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42. Calculate crude and standardized death rates for the Local population from the following data and compare them with crude death rate of the standard population (use both direct and indirect method).

Age	Standard	Deaths	Local	Deaths
group	Population		Population	
0-10	600	18	400	16
10-20	1000	5	1500	6
20-60	3000	24	2400	24
60-100	400	20	700	21

43. Below are given the figures of production (in thousand quintals) of a sugar factory:

Year	2001	2002	2003	2004	2005	2006	2007
Production	80	90	92	83	94	99	92

- (a) Fit a straight line trend to these figures.
- (b) Plot these figures on a graph and show the trend line.
- 44. Compute Laspeyre's, Paasche's and Fisher's index number for the following data.

Price		rice	Quantity		
Year	Base	Current	Base	Current	
	Year	Year	Year	Year	
А	20	40	8	6	
В	50	60	10	5	
С	40	50	15	15	
D	20	20 🧋	20	25	

 $(2 \times 15 = 30 \text{ Marks})$

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Name :

Fifth Semester B.Sc. Degree Examination, December 2022

First Degree Programme under CBCSS

Statistics

Core Course V

ST 1541 - LIMIT THEOREMS AND SAMPLING DISTRIBUTIONS

(2018 Admission onwards)

Time : 3 Hours

Max. Marks: 80

Statistical Table is permitted

SECTION - A

Answer all questions. Each question carries 1 mark.

- 1. Define sigma field.
- 2. If $A \subseteq B$ prove $P(A) \leq P(B)$, using axioms of Probability.

3. Define convergence in probability.

- 4. State Weak law of large numbers.
- 5. Define Chi square distribution with n degrees of freedom.
- 6. What is sampling distribution?
- 7. Define non central t distribution.
- 8. What is the relation between Student's t and F distribution?

- 9. Define r^{th} order statistic $X_{(r)}$.
- 10. If $X_1, X_2, ..., X_n$ be a random sample from U(0, θ), find the distribution function of Max($X_1, X_2, ..., X_n$).

 $(10 \times 1 = 10 \text{ Marks})$

SECTION - B

Answer any eight questions. Each question carries 2 marks

- 11. Define limit supremum and limit infimum for a sequence of events $\{A_n\}$.
- 12. Suppose $\{X_n\}$ is a sequence of random variables with probability mass function

 $P(X_n = 1) = \frac{1}{n} \text{ and } P(X_n = 0) = 1 - \frac{1}{n}$. Examine the convergence of $\{X_n\}$ in probability.

- 13. State Borel Cantelli lemma.
- 14. What are the assumptions on Central Limit theorem?
- 15. A random variable X has mean 50 and variance 100. Use Chebychev's inequality to obtain the upper bound for $P\{|X-50| \ge 15\}$.
- 16. List the advantages of Chebychev's inquality.
- 17. Let $X_1, X_2, ..., X_{100}$ be a random sample of size 100 drawn from a population with mean 10 and variance 9, then find $P(\overline{X} > 10.5)$ using central limit theorem.
- 18. Distinguish between parameter and statistic.

- 19. If the sample values are 1, 3, 5, 6, 9, find the standard error of the sample mean.
- 20. If $X_1, X_2, ..., X_n$ are independent $N(\mu, \sigma^2)$ random variables, find the distribution of $\sum_{i=1}^n \left(\frac{X_1 \mu}{\sigma}\right)^2$.
- 21. Find the mode of the Chi-square distribution with n degrees of freedom.
- 22. What are the characteristics of t distribution?
- 23. What are the properties of non central F distribution?
- 24. Let X and Y be independent standard normal variates. State the distribution of $\frac{x^2}{y^2}$ and write down the pdf.
- 25. Let $(X_1, X_2...X_n)$ be a random sample of size n from a distribution with density function f(x) and distribution function F(x). Write down the distribution function and probability density function of the nth order statistic, $X_{(n)}$.
- 26. Le $(X_1, X_2...X_n)$ be a sequence of independent normal random variables with pdf $f(x) = e^{-(x-\theta)}, x > \theta$. Find the pdf of $Min(X_1, X_2...X_n)$.

$$(8 \times 2 = 16 \text{ Marks})$$

SECTION - C

Answer any six questions. Each question carries 4 marks.

27. If $A_1, A_2, ..., A_n$... is a sequence of events in sample space S such that $A_1 \subseteq A_2 \subseteq ... \subseteq A_n$... then prove that $P\left(\bigcup_{n=1}^{\infty} A_n\right) = \lim_{n \to \infty} P(A_n)$.

- Show by an example that a sequence of distribution functions need not always converge to a distribution function.
- 29. State and prove Bernoulli's law of large numbers.
- 30. Examine whether the weak law of large numbers holds good for the sequence $\{X_n\}$ of independent random variables where $P\left\{X_n = \frac{1}{\sqrt{n}}\right\} = \frac{2}{3}, P\{X_n = -\frac{1}{\sqrt{n}}\} = \frac{1}{3}.$
- 31. A random sample of size 16 is taken from a normal population with mean 30 and variance 64. Find the probability that the sample variance s² will be less than the population variance.
- 32. Give the properties of Chi square distribution and examine its relationship with the normal distribution.
- 33. What are the mean and variance of sample variance s^2 ?
- 34. If X₁, X₂, X₃ and X₄ are independent observations from a univariate normal with mean zero and unit variance. Find the distribution of (a) $U = \frac{\sqrt{2} x_3}{\sqrt{x_1^2 + x_2^2}}$ (b) $V = \frac{3x_4^2}{x_1^2 + x_2^2 + x_3^2}$.
- 35. If two independent random samples of sizes 15 and 20 are taken from $N(\mu, \sigma)$, what is $P\left(\frac{s_1^2}{s_2^2} < 2\right)$?
- 36. Give two examples of a statistic following Students *t* distribution.
- 37. Using Statistical table, find the right tailed critical value corresponding to area 0.05 for (a) Chi-square distribution with 15 degrees of freedom (b) *t* distribution with 16 degrees of freedom.

38. Let X1, X2, ..., X_n be n independent variates, X_i having Geometric distribution with parameter p_i , *i.e.*, $P(X_i = x_i) = q_i^{x_i-1}p_i$, $q_i = 1 - p_i$, $x_i = 1, 2, 3, ...$ Show that $X_{(1)}$ is distributed geometrically with parameter $(1 - q_1q_2...,q_n)$.

 $(6 \times 4 = 24 \text{ Marks})$

SECTION - D

Answer any two questions. Each question carries 15 marks.

- 39. (a) State and prove Lindberg-Levy form of central limit theorem.
 - (b) Show by using central limit theorem that if X follows the binomial distribution with parameters (n, p), its distribution will tend to normal as $n \rightarrow \infty$.
- 40. (a) State and prove Chebychev's inequality.
 - (b) For the geometric distribution f(x)=2^{-x}, x = 1,2,3... prove that Chebychev's inequality gives P{|X-2|≤2} > 1/2, while the actual probability is 15/16.
- 41. (a) Derive the sampling distribution of means of samples chosen from a normal population.
 - (b) A population is known to follow normal distribution with mean 2 and S.D. 3. Find the probability that the mean of a sample size 16 taken from this population will be greater than 2.5.
- 42. (a) Derive the moment generating function of Chi square distribution with n degrees of freedom and hence obtain its mean and variance.
 - (b) State and prove the additive property of Chi square distribution.

- 43. (a) Define t, χ^2 and F statistics and establish relationship between each of them.
 - (b) If F (m, n) represents a F variate with (m, n) degrees of freedom, prove that $P[F(m,n) \ge c] = \left[F(n,m) \le \frac{1}{c} \right]$
- 44. Let $X_1, X_2, ..., X_n$ be a random sample from a population with cumulative density. Show that $Y_1 = Min (X_1, X_2, ..., X_n)$ is exponential with parameter $n\lambda$ if and only if each X_i is exponential with parameter λ .

(2 × 15 = 30 Marks)

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Statistics

Core Course VI

ST 1542 – ESTIMATION

(2018 Admission onwards)

Time : 3 Hours

SECTION A

Answer all questions. Each question carries 1 mark.

- 1. Define estimator.
- 2. Give an example of unbiased estimator.
- 3. Give the large sample property of a good estimator.
- 4. Define parametric space.
- 5. Give an example of a sufficient statistics.
- 6. Define minimum variance unbiased estimator.
- 7. Describe linear parametric function.
- 8. Define confidence coefficient.
- 9. Define likelihood function.
- 10. Define maximum likelihood estimator.

$(10 \times 1 = 10 \text{ Marks})$

P.T.O.

Max. Marks : 80

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SECTION B

Answer any eight questions. Each question carries 2 marks.

- 11. What do you understand by point estimation?
- 12. If *T* is an unbiased estimator of θ , examine whether T^2 is unbiased estimator of θ^2 .
- 13. State Neymann's factorization theorem and mention its uses.
- 14. Show that in Cauchy distribution.

$$f(\mathbf{x}, \theta) = \frac{1}{\pi \left[1 + (\mathbf{x} - \theta)^2\right]}, -\infty < \mathbf{x} < \infty$$

Sample median is a consistent estimator of θ .

- 15. Find sufficient estimator of θ in $f(x, \theta) = \theta e^{-\theta x}$, x > 0, $\theta > 0$ if it exist.
- 16. What is sampling distribution?
- 17. Find the maximum likelihood estimator of λ in $P(\lambda)$.
- 18. Explain the method of construction of confidence interval.
- 19. Describe linear estimation.
- 20. Give any two important properties of moment estimator.
- 21. Find 95% confidence interval of population proportion.
- 22. Describe minimum variance bound estimator.
- 23. Describe the method of least squares.
- 24. Explain estimability.
- 25. Find the consistent estimator of population mean in normal population.
- 26. If $(x_1, x_2, ..., x_n)$ is a random sample drawn from $N(\mu, 1)$ show that $t = 1/n \xi^n x^2$ is unbiased estimator of $\mu^2 + 1$.

 $(8 \times 2 = 16 \text{ Marks})$

2

SECTION C

Answer any **six** questions. Each question carries 4 marks.

- 27. State and prove the sufficient set of conditions for consistency of an estimator.
- 28. Let (X_1, X_2, X_3) be a random sample of size three drawn from a population with mean μ and variance σ^2 . Let T_1 , T_2 and T_3 be three estimators of μ . Where

 $T_1 = X_1 + X_2 - X_3$; $T_2 = 2X_1 + 3X_2 - 4X_3$; $T_3 = (X_1 + X_2 + X_3)/3$

- (a) Examine whether T_1 , T_2 and T_3 are unbiased estimators of μ or not.
- (b) Which estimator is more efficient? Why?
- 29. Show that minimum variance unbiased estimator is unique.
- 30. Find a sufficient estimator of θ based on a random sample of size *n* drawn from uniform distribution with parameter θ .
- 31. A random sample (x_1, x_2, \dots, x_n) is taken from $N(0, \sigma^2)$. Examine whether t = 1/n $\xi^n x_i^2$ is a minimum variance bound estimator of σ^2 .
- 32. Explain Gauss-Markov set-up.
- 33. Obtain 100 (1α) % confidence interval of σ^2 based on sample observations drawn from $N(\mu, \sigma^2)$.
- 34. A random sample of 500 apples was taken from a large consignment and 60 were found to be bad apples. Find 98% confidence interval for the proportion of bad apples in the consignment.
- 35. Explain the desirable properties of a good estimator.
- 36. Examine whether sample variance is an unbiased and consistent estimator of population variance in $N(\mu, \sigma^2)$.
- 37. Obtain the moment estimator of θ based on sample observations drawn from

 $f(\mathbf{x},\theta) = \theta \, e^{-\theta \mathbf{x}}, \, \mathbf{x} > 0, \, \theta > 0.$

38. State and establish the necessary and sufficient condition for estimability of a linear parametric function.

 $(6 \times 4 = 24 \text{ Marks})$

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SECTION D

Answer any two questions. Each question carries 15 marks.

- 39. (a) Discuss the method of maximum likelihood estimation. Also describe any two important properties of M.L.E.
 - (b) Obtain the maximum likelihood estimators of μ and σ^2 in $N(\mu, \sigma^2)$.
- 40. (a) Describe the method of moments. Examine whether moment estimators are
 - (i) unbiased
 - (ii) unique.
 - (b) Find the moment estimators of α and β in

$$f(x, \alpha, \beta) = \frac{\beta^2}{\alpha} e^{-\beta x} X^{\alpha-1}, 0 < x < \infty,$$

- 41. (a) Let X₁, X₂, X₃,.....X_n be a random sample of size n drawn from a population with f(x,θ) = e^{-(x-θ)}, 0 < x < ∞, -∞ < θ < ∞
 Find sufficient estimator of θ.
 - (b) Obtain the minimum variance bound estimator of μ in $N(\mu, \sigma^2)$ when σ^2 is known. Also find the variance of the estimator.
 - (c) Find an unbiased estimator of θ in $f(x,\theta) = \theta(1-\theta)^{x-1}$, $x = 1, \infty, \dots, 0 < \theta < 1$.
- 42. (a) Obtain the 100 $(1-\alpha)$ % confidence interval of $P_1 P_2$, where P_1 and P_2 are proportions of two independent populations.
 - (b) Show that for the distribution $f(x, \theta) = \theta e^{-\theta x}$, x > 0 the central confidence limits for large samples with 95% confidence coefficient are given by $\left(1 \pm \frac{1.96}{\sqrt{n}}\right)/\overline{x}$.
- 43. Find 100 $(1-\alpha)$ % confidence interval of $\mu_1 \mu_2$, where μ_1 and μ_2 are means of two independent normal populations when
 - (a) the population variances are unknown and different.
 - (b) when the population variances are common and unknown.
- 44. State and prove Gauss-Markov's theorem.

 $(2 \times 15 = 30 \text{ Marks})$

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(Pages : 6)

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Statistics

Core Course VII

ST 1543 – TESTING OF HYPOTHESIS

(2018 Admission onwards)

Time : 3 Hours

Max. Marks: 80

(Statistical Table and Calculator and permitted)

SECTION - A

Answer all questions. Each question carries 1 mark.

- 1. What is a simple hypothesis?
- 2. What do you mean by best critical region?
- 3. Define the power of a test.
- 4. What do you mean by most powerful test?
- 5. What are likelihood ratio tests?
- What are the conditions to be satisfied to apply a Chi-square test for goodness of fit.

- 7. Which test statistics is used to test for a hypothetical value of the proportion of observations when a sample is taken from a Binomial population?
- 8. What are the assumptions of a t-test?
- 9. Define the empirical distribution function.
- 10. What is the indication of the number of runs in a run test?

 $(10 \times 1 = 10 \text{ Marks})$

SECTION - B

Answer any eight questions. Each question carries 2 marks.

- 11. Distinguish between the level of the test α and the p value.
- 12. A population follows Normal distribution with parameters μ and σ = 3. To test the hypothesis H₀ = μ = 5 vs H₁: μ = 7, the test procedure suggested is to reject H₀ if x̄ ≥ 6 where x̄ is the mean of a sample of size 16. Find the significance level and power of the test.
- 13. What are the steps for carrying out a statistical test procedure?
- 14. Using the Neymann-Pearson Lemma, find the best critical region for the test $H_0: \mu \approx \mu_0 \text{ vs } H_1: \mu = \mu_1$, when μ_1 and σ^2 is known.
- 15. When do you call a test uniformly most powerful?
- 16. A coin is tossed 900 times in which head appears 490 times. Does it support the claim that the coin is unbiased?
- 17. Outline the large sample test for testing the specified variance of the population.

- 18. From a population with mean 200 and unknown SD, a sample is taken with mean 195 and S.D 50.If the null hypothesis is rejected at 5% level, what is the least sample size?
- 19. Discuss the applications of chi-square distribution.
- 20. Briefly discuss the test procedure of testing the equality means of the population with small samples.
- 21. The S.Ds of two samples of sizes 10 and 14 from two normal populations are 3.5 and 3.0 respectively. Examine whether the two populations have the same variances.
- 22. Define an F statistic. What are its uses?
- 23. In two Colleges affiliated to a University 40 out of 250 and 49 out of 200 students failed in an examination. If the overall percentage of failure in the University is 20, examine whether the two Colleges differ in performance significantly.
- 24. Discuss the runs test for randomness.
- 25. What is the procedure of a sign test for one sample?
- 26. Explain the Mann-Whitney U test. For which parametric test this is an alternative?

(8 × 2 = 16 Marks)

SECTION - C

Answer any six questions. Each question carries 4 marks.

27. Let $X \sim N$ $(\mu, \sigma^2), \mu$ is the unknown mean and $\sigma^2 = 4$. To test $H_0: \mu = -1 vs H_1: \mu = 1$ based on a sample of size 10 from this population, we use the critical region $x_1 + 2x_2x + 3x_3 + ... + 10x_{10} \ge 0$. What is its size? What is the power of the test?

- 28. State the Neyman-Pearson lemma and give its relevance.
- 29. Examine whether a Best Critical Region exists for testing $H_0: \theta = \theta_0, vs H_1: \theta > \theta_0$ for the parameter θ of $f(x; \theta) = \frac{1+\theta}{(x+\theta)^2}, 1 \le x < \infty$.
- 30. Mention the properties of likelihood ratio test.
- 31. A sample of 400 observations were taken from a population with S.D 15. If the mean of the sample is 27, test whether the hypothesis that the population mean is greater than 24.
- 32. A manufacturer of dry cells claimed that the life of their cells is 24.0 hours. A sample of 10 cells had mean life of 22.5 hours with a S.D 3.0 hours. On the basis of this information test whether the claim is valid or not.
- 33. Write the procedure for carrying out a chi-square test of homogeneity.
- 34. Test whether the following figures provide the evidence of the effectiveness on inoculation.

	Attacked	Not attacked
Inoculated	120	80
Not Inoculated	180	420

- 35. Two samples of 6 and 5 items respectively gave the following data: mean of the first sample =40,S.D of the first sample =8, mean of the second sample = 50 S.D of the second sample =10. Is the difference in means significant at 5% level?
- 36. What are the advantages and disadvantages of non-parametric methods over parametric methods?

- 37. A public school official felt that high school sections of a large school system would tend to score higher on a standard reading examination than the national median of 50. He randomly select 13 students and gave them the test. The results are as follows:57,70,42,48,72,63.45,66,59,39,73,78,47. Is his feeling correct? Use Wilcoxon's signed rank test. (From tables with n=13, α = .01 table value C=13).
- Write a comparison between Chi-square test of goodness-of—fit and a Kolmogrov-Smirnov test.

(6 × 4 = 24 Marks)

SECTION – D

Answer any two questions. Each question carries 15 marks.

- 39. (a) Show that every most powerful critical region is unbiased.
 - (b) Given a random sample of size n from a population with pdf $f(x,\sigma) = \frac{1}{\sigma}e^{-\frac{x}{\sigma}}, x > 0, \sigma > 0$. Show that there exists no UMP test for testing $H_0: \sigma = \sigma_0, vsH_1: \sigma \neq \sigma_0$.
- 40. (a) Give the procedure for testing the equality of means of two normal populations when the population variances are known.
 - (b) Two independent samples from two Normal populations are shown below. Test whether the two populations have the same variance.

Sample I 60 65 71 74 76 82 85 87 Sample II 61 66 67 85 78 63 85 86 88 91

- 41. (a) A sample of 27 pairs of observations from a Normal population gives the sample correlation coefficient r = 0.6. Is it likely that the variables are correlated?
 - (b) Discuss the test for equality of correlation coefficients of two populations.

- 42. (a) Explain the paired t test, mentioning the assumptions involved.
 - (b) An IQ test was administered to 5 persons before and after they were trained. The results are as follows:

Candidate :	А	В	С	D	Е
IQ before training :	110	120	123	132	125
IQ after training :	120	118	125	136	121

Test whether there is any change in IQ after the training.

- 43. (a) Discuss the test for equality of means of two normal populations(i) with known S,Ds and (ii) with the same but unknown S.D.
 - (b) Two samples from normal populations gave the following results.

Sample size	Mean	S.D.
12	1050	68
10	980	74

Do the samples come from the same population with $\sigma_1^2 = \sigma_2^2$, unknown.

44. (a) Explain the Kolmogrov-Smirnov one sample test procedure.

(b) Discuss the procedure of the Wilcoxon's matched pair signed rank test.
 (2 × 15 = 30 Marks)

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Core Course VIII

ST 1544 – SAMPLE SURVEY METHODS

(2018 Admission onwards)

Time : 3 Hours

Max. Marks: 80

SECTION - A

Answer all questions. Each question carries 1 mark.

- 1. Define sampling frame.
- 2. What are the objectives of sampling?
- 3. Mention some situations in which sampling methods alone can be adopted to collect data.
- 4. What is meant by purposive/subjective sampling?
- 5. Discuss the problem of non-response in a Sample Survey.
- 6. Name any two methods of selecting simple random samples.
- 7. Define finite population correction.
- 8. When do you go for stratification?

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- 9. Define a circular systematic sample.
- 10. Describe the use of auxiliary information in sampling.

SECTION - B

$(10 \times 1 = 10 \text{ Marks})$

Answer any eight questions. Each question carries 2 marks.

- 11. What do you mean by Judgment sampling?
- 12. Distinguish between standard error and standard deviation.
- 13. How can one estimate the population total and its variance?
- 14. What do you mean by Mean Square Error? When do you use it?
- 15. Explain the errors in sampling.
- 16. How do you determine the sample size in SRSWOR.
- 17. Define a Simple Random Sample With Replacement (SRSWR).
- 18. Highlight the advantages of stratification.
- 19. What do you mean by proportional allocation in stratified sampling?
- 20. What do you mean by post stratification? Will it increase the precision of the estimate? Establish your claim.
- 21. What is balanced systematic sample.
- 22. What are the disadvantages of systematic sampling?
- 23. Distinguish between stratified sampling and cluster sampling.
- 24. What is meant by difference estimator?
- 25. What are the two types of ratio estimates in Stratified sampling?
- 26. What is meant by linear regression estimator for the population mean?

(8 × 2 = 16 Marks)

SECTION - C

Answer any six questions. Each question carries 4 marks.

- 27. Define snowball sampling. In which situation it is used?
- 28. What are the advantages and disadvantages of sampling over census?
- 29. Show that in SRS $P_{ir} = \frac{1}{N}$, where P_{ir} denotes the probability of selecting the ith unit in the rth draw in a population of size N.
- 30. In SRSWR, show that an estimate based on d distinct units is superior to the one based on n units (d <n).
- 31. Establish that in SRSWOR, the sample mean square is an unbiased estimate of the population mean square.
- 32. Compare the efficiency of Systematic Sample with SRSWOR in terms of the intra

class correlation coefficient.

- 33. Obtain the expression for the sample size n_i for the ith stratum under optimum allocation in stratified random sampling assuming a suitable cost function.
- 34. Explain Neymann's allocation in stratified sampling and derive the variance of the population total.
- 35. Give an unbiased estimate of the population proportion and its unbiased estimated variance when random sampling is with stratification.
- 36. In a linear systematic sample for N = nk, show that the sample mean is an unbiased estimator of the population mean.
- 37. Distinguish between Ratio estimate and linear regression estimate.
- 38. Show that the ratio estimators are biased.

 $(6 \times 4 = 24 \text{ Marks})$

SECTION - D

Answer any two questions. Each question carries 15 marks.

- 39. Discuss briefly on the organizational aspects of a sampling survey pointing out the pros and cons.
- 40. Show that the sample mean \overline{y} is an unbiased and consistent estimate of the population mean in SRS and show that $V_{SRSWOR}(\overline{y}) = \frac{N-n}{N-1}V_{SRSWR}(\overline{y})$.
- 41. Briefly explain the precision of the estimate of the population mean under any three basic probability sampling methods.
- 42. For populations with a linear trend, prove with usual notations

 $V(\overline{y}_{st}):V(\overline{y}_{sy}):V(\overline{y}_{ran})=\frac{1}{n}:1:n.$

- 43. Define linear systematic sampling. Show that the higher heterogeneity makes the estimator more efficient in a linear systematic sample.
- 44. Compare the efficiency of the regression estimator with those based on mean per unit and ratio estimation procedure.

 $(2 \times 15 = 30 \text{ Marks})$